Key information on – maxon DC motor and maxon EC motor

The motor as an energy converter

The electric motor converts electrical power $P_{el}$ (current $I$ and voltage $U$) into mechanical power $P_{mech}$ (speed $n$ and torque $M$). The losses that arise are divided into frictional losses, attributable to $P_{mech}$ and in Joule power losses $P_{J}$ of the winding (resistance $R$). Iron losses do not occur in the coreless maxon DC motors. In maxon EC motors, they are treated formally like an additional friction torque. The power balance can therefore be formulated as:

$$P_{el} = P_{mech} + P_{J}$$

The detailed result is as follows:

$$U \cdot I = \frac{\pi}{30 000} \cdot n \cdot M + R \cdot I^2$$

Electromechanical motor constants

The geometric arrangement of the magnetic circuit and winding defines in detail how the motor converts the electrical input power (current, voltage) into mechanical output power (speed, torque). Two important characteristic values of this energy conversion are the speed constant $k_n$ and the torque constant $k_M$.

The speed constant combines the speed $n$ with the voltage induced in the winding $U_{ind}$ (=EMF). $U_{ind}$ is proportional to the speed; the following applies:

$$n = k_n \cdot U_{ind}$$

Similarly, the torque constant links the mechanical torque $M$ with the electrical current $I$.

$$M = k_M \cdot I$$

The core statement of this proportionality is that the variables torque and current are equivalent for the maxon motors.

Motor diagrams

A diagram can be drawn for every maxon DC and EC motor, from which key motor data can be taken. Although tolerances and temperature influences are not taken into consideration, the values are sufficient for a first estimation in most applications. In the diagram, speed $n$, current $I$, output power $P_2$ and efficiency $\eta$ are drawn as a function of the torque $M$.

Speed-torque line

This curve describes the mechanical behavior of the motor at a constant voltage $U$:

- Speed decreases linearly with increasing torque.
- The faster the motor turns, the less torque it can provide.

The curve can be described with the help of the two end points, no-load speed $n_0$ and stall torque $M_H$ (cf. lines 3 and 4 in the motor data). DC motors can be operated at any voltage. No-load speed and stall torque change proportionally to the applied voltage. This is equivalent to a parallel shift of the speed-torque line in the diagram.

Between the no-load speed and voltage, the following proportionality applies in good approximation

$$n_0 = k_{n0} \cdot U$$

where $k_{n0}$ is the speed constant (line 15 of the motor data).

Independent of the voltage, the speed-torque line is described most practically by the slope or gradient of the curve (line 5 of the motor data).

$$\frac{\Delta n}{\Delta M} = \frac{n_0}{M_0}$$

Derivation of the speed-torque line

The following occurs if one replaces current $I$ with torque $M$ using the torque constant in the detailed power balance:

$$U - \frac{M}{k_M} = \frac{\pi}{30 000} \cdot n \cdot M + R \left( \frac{M}{k_M} \right)^2$$

Transformed and taking account of the close relationship of $k_M$ and $k_n$, an equation is produced of a straight line between speed $n$ and torque $M$.

$$n = k_n \cdot U - \frac{30 000}{\pi} \cdot \frac{R}{k_M} \cdot M$$

or with the gradient $\frac{\Delta n}{\Delta M}$ and the no-load speed $n_0$.

$$n = n_0 - \frac{\Delta n}{\Delta M} \cdot M$$

Units

In all formulas, the variables are to be used in the units according to the catalog (cf. physical variables and their units on page 40).

The following applies in particular:

- All torques in mNm
- All currents in A (even no-load currents)
- Speeds (rpm) instead of angular velocity (rad / s)
The speed-torque gradient is one of the most informative pieces of data and allows direct comparison between different motors. The smaller the speed-torque gradient, the less sensitive the speed reacts to torque (load) changes and the stronger the motor. With the maxon motor, the speed-torque gradient within the winding series of a motor type (i.e. on one catalog page) remains practically constant.

**Current curve**
The current curve represents the equivalence of current and torque: the more current that flows through the motor, the more torque is produced. The current curve can be easily drawn through the two end points no-load current $I_0$ and starting current $I_A$ (lines 6 and 7 of the motor data). The no-load current is equivalent to the friction torque $M_R$, that describes the internal friction in the bearings and commutation system. $M_R = k_{IR} \cdot I_0$

In the maxon EC motor, there are strong, speed dependent iron losses in the stator iron stack instead of friction losses in the commutation system.

The motors develop the highest torque when starting. It is many times greater than the normal operating torque, so the current uptake is the greatest as well.

The following applies for the stall torque $M_s$ and starting current $I_A$:

$M_s = k_{IS} \cdot I_A$

**Output power curve**
The mechanical output power $P_2$ is calculated from the speed $n$ and the torque $M$

$P_2 = \frac{\pi}{30,000} n \cdot M$

In the speed-torque diagram, the output power is equivalent to the area of the rectangle below the speed-torque line. This rectangle and, thus, the output power, is greatest at half stall torque and half no-load speed. The power curve is a parabola, whose maximum value (line 12 of the motor data) depends quadratically on the applied motor voltage.

**Efficiency curve**
The efficiency $\eta$ describes the relationship of mechanical power delivered to electrical power consumed.

$\eta = \frac{\pi}{30,000} \frac{n \cdot M}{U \cdot I}$

One can see that at constant applied voltage $U$ and due to the proportionality of torque and current, the efficiency increases with increasing speed (decreasing torque). At low torques, friction losses become increasingly significant and efficiency rapidly approaches zero. Maximum efficiency (line 13 of motor data) is calculated using the starting current and no-load current and is dependent on voltage

$\eta_{max} = \left(1 - \frac{U_s}{U}ight)^2$

A rule of thumb is that maximum efficiency occurs at roughly one seventh of the stall torque. This means that maximum efficiency and maximum output power do not occur at the same torque.
Operating ranges: the limits of the motor

In the catalog, there is a diagram that covers the winding range for every maxon DC and EC motor type. The limits of the operating ranges are:

**The maximum permissible speed**

is primarily limited by the commutation system. The commutator and brushes wear more rapidly at very high speeds. The reasons are:

- Increased mechanical wear because of the large traveled path of the commutator
- Increased electro-erosion because of brush vibration and spark formation.

A further reason for limiting the speed is the rotor’s residual mechanical imbalance which shortens the service life of the bearings. Higher speeds than the limit speed \( n_{\text{max}} \) (line 9) are possible, however, they are “paid for” by a reduced service life expectancy.

**Maximum continuous current, maximum continuous torque**

Due to the maximum winding temperature, a maximum current must not be exceeded in continuous operation. The heat produced must be able to dissipate and the maximum rotor temperature should not be exceeded. This results in a maximum continuous current \( I_{\text{cont}} \) (line 10 of the motor data), at which the maximum winding temperature is attained under standard conditions (25°C ambient temperature, no heat dissipation via the flange, free air circulation). Higher motor currents cause excessive winding temperatures.

The maximum continuous current is heavily dependent on the winding. Thin wire windings have smaller continuous currents than thick wire windings. In the case of low-resistance windings, the current bearing ability of the commutation system further limits the continuous current. Based on the equivalence of the motor current and torque, each motor is assigned a maximum continuous torque (line 11 of the motor data). It is practically constant within the winding series of a motor type and represents a characteristic parameter for each motor type.

**Permanent operating range**

The two criteria “maximum continuous torque” and “maximum permissible speed” limit the continuous operating range. Operating points within this range are not critical thermally and do not generally cause increased wear of the commutation system. For many DC motors, it is recommended for service life reasons that the speed limit should not be fully exploited, but the motor operated below the nominal voltage instead. This operating range is called the recommended operating range.

**Short-term operating range**

The motor may only be loaded with the maximum continuous current for thermal reasons. However, temporary higher currents (torques) are allowed. As long as the winding temperature is below the critical value, the winding will not be damaged.

Phases with increased currents are time limited. A measure of how long the temporary overload can last is provided by the thermal time constant of the winding (line 21 of the motor data). The magnitude of the times with overload ranges from several seconds for the smallest motors (10 mm to 13 mm diameter) up to roughly one minute for the largest (80 mm, 75 mm diameter). The calculation of the exact overload time is heavily dependent on the motor current and the rotor’s starting temperature.

In order not to overload the commutation system, it is recommended that the speed be reduced with increasing overload. The upper limit of the short-term operating range is, therefore, formed by a hyperbola of constant mechanical power.

**Maximum winding temperature**

The motor current causes the winding to heat up due to the winding’s resistance. To prevent the motor from overheating, this heat must dissipate to the environment via the stator. The coreless winding is the thermally critical point. The maximum rotor temperature must not be exceeded, even temporarily. With graphite brush motors which tend to have higher current loads, the maximum rotor temperature is 125°C (in individual cases up to 155°C). Motors with precious metal commutators only allow lower current loads, so that the rotor temperatures must not exceed 85°C.

Favourable mounting conditions, such as good air circulation or cooling plates, can significantly lower temperatures.

**Operating ranges of the maxon EC motor**

The maximum permissible speed is calculated using the service life considerations of the ball bearings (at least 20 000 hours) at the maximum residual unbalance of the rotor.

The limit of the continuous operating range is formed by the maximum winding temperature. With increasing speed eddy current losses grow in the magnetic return, causing additional heating. Thus, at higher speeds, the maximum continuous current and the maximum continuous torque decrease.
Acceleration

In accordance with the electrical boundary conditions (power supply, control, battery), a distinction is principally made between two different starting processes:
- Start under constant voltage (without current limitation)
- Start under constant current (with current limitation)

Start with constant terminal voltage
Here, the speed increases from the stall torque along the speed-torque line. The greatest torque and thus the greatest acceleration is effective at the start. The faster the motor turns, the lower the acceleration. The speed increases more slowly. This exponentially flattening increase is described by the mechanical time constant $\tau_m$ (line 16 of the motor data). After this time, the rotor at the free shaft end has attained 63% of the no-load speed. After roughly three mechanical time constants, the rotor has almost reached the no-load speed.

Several useful formulas for acceleration
(all variables in units according to the catalog)

Under constant voltage:
- Mechanical time constant $\tau_m$ (in ms) of the unloaded motor:
  \[ \tau_m = 100 \cdot \frac{J_m R}{k_u} \]
- Mechanical time constants $\tau_m'$ (in ms) with an additional load inertia $J_L$:
  \[ \tau_m' = 100 \cdot \frac{J_m R}{k_u} \left( 1 + \frac{J_L}{J_m} \right) \]
- Maximum angular acceleration $\omega_{\text{max}}$ (in rad / s$^2$) of the unloaded motor:
  \[ \omega_{\text{max}} = 10^4 \cdot \frac{M_u}{J_m} \]
- Maximum angular acceleration $\omega_{\text{max}}$ (in rad / s$^2$) with an additional load inertia $J_L$:
  \[ \omega_{\text{max}} = 10^4 \cdot \frac{M_u}{J_m + J_L} \]
- Run-up time (in ms) at constant voltage up to the operating point $(M_u, n_u)$:
  \[ \Delta t = \tau_m' \cdot \ln \left( \frac{1 - M_u + M_i}{M_i} \cdot \frac{n_u}{n_i} \right) \]

Under constant current:
- Angular acceleration $\alpha$ (in rad / s$^2$) at constant current $I$ or constant torque $M$ with an additional load of inertia $J_L$:
  \[ \alpha = 10^4 \cdot \frac{k_u \cdot I}{J_m + J_L} = 10^4 \cdot \frac{M}{J_m + J_L} \]
- Run-up time $\Delta t$ (in ms) at a speed change $\Delta n$ with an additional load inertia $J_L$:
  \[ \Delta t = \frac{\pi}{300} \cdot \Delta n \cdot \frac{J_m + J_L}{k_u \cdot I} \]
Thermal behavior

The Joule power losses P_J in the winding determine heating of the motor. This heat energy must be dissipated via the surfaces of the winding and motor.

The increase $\Delta T_W$ of the winding temperature $T_W$ with regard to the ambient temperature arises from heat losses $P_J$ and thermal resistances $R_{th1}$ and $R_{th2}$.

$$T_W - T_A = \frac{P_J}{R_{th1} + R_{th2}}$$

Here, thermal resistance $R_{th1}$ relates to the heat transfer between the winding and the stator (magnetic return and magnet), whereas $R_{th2}$ describes the heat transfer from the housing to the environment. Mounting the motor on a heat dissipating chassis noticeably lowers thermal resistance $R_{th2}$. The values specified in the data sheets for thermal resistances and the maximum continuous current were determined in a series of tests, in which the motor was end-mounted onto a vertical plastic plate. The modified thermal resistance $R_{th2}$ that occurs in a particular application must be determined using original installation and ambient conditions.

The heating runs at different rates for the winding and stator due to the different masses. After switching on the current, the winding heats up first (with time constants from several seconds to half a minute). The stator reacts much slower, with time constants ranging from 1 to 30 minutes depending on motor size. A thermal balance is gradually established. The temperature difference of the winding compared to the ambient temperature can be determined with the value of the current $I$ (or in intermittent operation with the effective value of the current $I_{rms}$).

$$\Delta T_W = \frac{(R_{th1} + R_{th2}) \cdot R \cdot \Delta F}{1 - \alpha_{Cu} \cdot (R_{th1} + R_{th2}) \cdot R \cdot \Delta F}$$

Here, electrical resistance $R$ must be applied at the actual ambient temperature.

Influence of temperature

An increased motor temperature affects winding resistance and magnetic characteristic values.

Winding resistance increases linearly according to the thermal resistance coefficient for copper: $(\alpha_{Cu} = 0.00392/\degree C)$:

$$R_t = R_{25} \cdot (1 + \alpha_{Cu} (T - 25 \degree C))$$

Example: a winding temperature of 75°C causes the winding resistance to increase by nearly 20%.

The magnet becomes weaker at higher temperatures. The reduction is 1 to 10% at 75°C depending on the magnet material.

The most important consequence of increased motor temperature is that the speed curve becomes steeper which reduces the stall torque. The changed stall torque can be calculated in first approximation from the voltage and increased winding resistance.

$$M_{st} = k_M \cdot I_{st} = k_M \cdot \frac{U}{R_t}$$
Motor selection

The drive requirements must be defined before proceeding to motor selection.
- How fast and at which torques does the load move?
- How long do the individual load phases last?
- What accelerations take place?
- How great are the mass inertias?

Often the drive is indirect, this means that there is a mechanical transformation of the motor output power using belts, gears, screws and the like. The drive parameters, therefore, are to be calculated to the motor shaft. Additional steps for gear selection are listed below.

Furthermore, the power supply requirements need to be checked.
- Which maximum voltage is available at the motor terminals?
- Which limitations apply with regard to current?

The current and voltage of motors supplied with batteries or solar cells are very limited. In the case of control of the unit via a servo amplifier, the amplifier’s maximum current is often an important limit.

Selection of motor types

The possible motor types are selected using the required torque. On the one hand, the peak torque, $M_{\text{max}}$, is to be taken into consideration and on the other, the effective torque $M_{\text{RMS}}$.

Continuous operation is characterized by a single operating point $(M_B, n_B)$. The motor types in question must feature a continuous torque, $M_{\text{cont}}$ that is larger than the operating torque $M_B$.

$$M_{\text{cont}} > M_B$$

Unlike continuous operation, in work cycles such as start / stop operation, the effective torque must be less than the motor’s continuous torque. This prevents the motor from overheating.

$$M_{\text{RMS}} > M_{\text{RMS}}$$

The stall torque of the selected motor should usually exceed the required peak torque.

$$M_I > M_{\text{max}}$$

Selection of the winding: electric requirement

In selecting the winding, it must be ensured that the voltage applied directly to the motor is sufficient for attaining the required speed in all operating points.

Unregulated operation

In applications with only one operating point, this is often achieved with a fixed voltage $U$. A winding is sought with a speed-torque line that passes through the operating point at the specified voltage. The calculation uses the fact that all motors of a type feature practically the same speed-torque gradient. A target no-load speed $n_{0,\text{theor}}$, is calculated from operating point $(n_B, M_B)$.

$$n_{0,\text{theor}} = \frac{n_B + \Delta n}{M_B} M_B$$

This target no-load speed must be achieved with the existing voltage $U$, which defines the target speed constant.

$$k_{n,\text{theor}} = \frac{n_{0,\text{theor}}}{U}$$

Those windings whose $k_n$ is as close to $k_{n,\text{theor}}$ as possible, will approximate the operating point the best at the specified voltage. A somewhat larger speed constant results in a somewhat higher speed, a smaller speed constant results in a lower one. The variation of the voltage adjusts the speed to the required value, a principle that servo amplifiers also use.

Motor current $I$ is calculated from the torque constant $k_M$ of the selected winding and the operating torque $M_B$.

$$I = \frac{M_B}{k_M}$$

Tips for evaluating the requirements:

- Often the load points (especially the torque) are not known or are difficult determine. In such cases you can operate your device with a measuring motor roughly estimated according to size and power.
- Vary the voltage until the desired operating points and motion sequences have been achieved. Measure the voltage and current flow. Using these specifications and the order number of the measuring motor, our engineers can often specify the suitable motor for your application.

Additional optimization criteria are, for example:
- Mass to be accelerated (type, mass inertia)
- Type of operation (continuous, intermittent, reversing)
- Ambient conditions (temperature, humidity, medium)
- Power supply, battery

When selecting the motor type, other constraints also play a major role?
- What maximum length should the drive unit have, including gear and encoder?
- What diameter?
- What service life is expected from the motor and which commutation system should be used?
- Precious metal commutation for continuous operation at low currents (rule of thumb for longest service life: up to approx. 50 % of $I_{\text{cont}}$)
- Graphite commutation for high continuous currents (rule of thumb: 50 % to approx. 75 % of $I_{\text{cont}}$) and frequent current peaks (start / stop operation, reversing operation).
- Electronic commutation for highest speeds and longest service life.
- How great are the forces on the shaft, do ball bearings have to be used or are less expensive sintered bearings sufficient?
Regulated servo drives
In work cycles, all operating points must lie beneath the curve at a maximum voltage \( U_{\text{max}} \). Mathematically, this means that the following must apply for all operating points \( (n_B, M_B) \):

\[
k_u : U_{\text{max}} = n_B > n_0 + \frac{\Delta n}{\Delta M} M_B
\]

When using servo amplifiers, a voltage drop occurs at the power stage, so that the effective voltage applied to the motor is lower. This must be taken into consideration when determining the maximum supply voltage \( U_{\text{max}} \). It is recommended that a regulating reserve of some 20 % be included, so that regulation is even ensured with an unfavorable tolerance situation of motor, load, amplifier and supply voltage.

Finally, the average current load and peak current are calculated ensuring that the servo amplifier used can deliver these currents. In some cases, a higher resistance winding must be selected, so that the currents are lower. However, the required voltage is then increased.

### Example for motor / gear selection

A drive should move cyclically in accordance with the following speed diagram.

The inertia of load \( J_L \) to be accelerated is 120,000 gcm\(^2\). The constant friction torque is 300 mNm. The motor is to be driven with the linear 4-Q servo amplifier from maxon (LSC). The power supply delivers max. 5 A and 24 V.

#### Calculation of load data

The torque required for acceleration and braking is calculated as (motor and gear inertia are ignored).

\[
M_t = J_L \cdot \alpha + J_L \cdot \frac{\Delta n}{\Delta M} = 0.012 \cdot \frac{60}{0.5} = 0.15 \text{ Nm} = 150 \text{ mNm}
\]

Together with the friction torque, the following torques result for the different phases of motion:

- Acceleration phase (duration 0.5 s) 450 mNm
- Constant speed (duration 2 s) 300 mNm
- Braking (friction helps braking) (duration 0.5 s) 150 mNm
- Standstill (duration 0.7 s) 0 mNm

Peak torque occurs during acceleration. The RMS determined torque of the entire work cycle is

\[
M_{\text{RMS}} = \sqrt{\frac{1}{T_{\text{tot}}} (t_1 M_1^2 + t_2 M_2^2 + t_3 M_3^2 + t_4 M_4^2)}
\]

\[
= \sqrt{\frac{1}{3.7} (0.5 \cdot 450^2 + 2 \cdot 300^2 + 0.5 \cdot 150^2 + 0.7 \cdot 0^2)} = 280 \text{ mNm}
\]

The maximum speed (60 rpm) occurs at the end of the acceleration phase at maximum torque (450 mNm). Thus, the peak mechanical power is.

\[
P_{\text{max}} = M_{\text{max}} \cdot n_{\text{max}} \cdot \frac{3 \pi}{10} = 0.45 \cdot 60 \cdot 0.15 = 2.8 \text{ W}
\]

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### Physical variables and their units

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<th>Description</th>
<th>Units</th>
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<td>i</td>
<td>Gear reduction*</td>
<td>A, mA</td>
</tr>
<tr>
<td>I</td>
<td>Motor current</td>
<td>A, mA</td>
</tr>
<tr>
<td>I_{\text{st}}</td>
<td>Starting current*</td>
<td>A</td>
</tr>
<tr>
<td>I_{\text{nl}}</td>
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<td>I_{\text{RMS}}</td>
<td>RMS determined current</td>
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<td>I_{\text{M}}</td>
<td>Maximum continuous current</td>
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<td>J_k</td>
<td>Moment of inertia of the rotor*</td>
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<td>Moment of inertia of the load</td>
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<td>Torque constant*</td>
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<tr>
<td>k_n</td>
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<tr>
<td>M</td>
<td>(Motor) torque</td>
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<td>M_{\text{op}}</td>
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<tr>
<td>M_{\text{M}}</td>
<td>Motor torque</td>
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<tr>
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<td>Maximum angle acceleration</td>
<td>rad / s²</td>
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<td>Curve gradient*</td>
<td>rpm / mNm</td>
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<td>Temperature difference winding/ambient</td>
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<tr>
<td>\eta</td>
<td>(Motor) efficiency</td>
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<td>\eta_{\text{g}}</td>
<td>(Gear) efficiency*</td>
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<td>Therm. Time constant of the winding*</td>
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</tbody>
</table>

(*Specified in the motor or gear data)
Gear selection

A gear is required with a maximum continuous torque of at least 0.28 Nm and an intermittent torque of at least 0.45 Nm. This requirement is fulfilled, for example, by a planetary gear with 22 mm diameter (metal version).

The recommended input speed of 6000 rpm allows a maximum reduction of

\[ i_{\text{max}} = \frac{n_{\text{max,G}}}{n_8} = \frac{6000}{60} = 100 : 1 \]

We select the three-stage gear with the next smallest reduction of 84 : 1 (stock program). Efficiency is max. 59 %.

Motor type selection

Speed and torque are calculated to the motor shaft

\[ n_{\text{rot}} = i \cdot n_8 = 84 \cdot 60 = 5040 \text{ rpm} \]

\[ M_{\text{rot,RMS}} = \frac{M_{\text{max}}}{i \cdot \eta } = \frac{280}{84 \cdot 0.59} \approx 5.7 \text{ mNm} \]

\[ M_{\text{rot, max}} = \frac{M_{\text{max}}}{i \cdot \eta } = \frac{450}{84 \cdot 0.59} \approx 9.1 \text{ mNm} \]

The possible motors, which match the selected gears in accordance with the maxon modular system, are summarized in the table opposite. The table only contains motors with graphite commutation which are better suited to start / stop operation.

Selection falls on an A-max 22, 6 W, which demonstrates a sufficiently high continuous torque. The motor should have a torque reserve so that it can even function with a somewhat unfavorable gear efficiency. The additional torque requirement during acceleration can easily be delivered by the motor. The temporary peak torque is not even twice as high as the continuous torque of the motor.

Selection of the winding

The motor type A-max 22, 6 W has an average speed-torque gradient of some 480 rpm / mNm. However, it should be noted that the two lowest resistance windings have a somewhat steeper gradient. The desired no-load speed is calculated as follows:

\[ n_{\text{th, max}} = n_{\text{max}} + \frac{\Delta n}{\Delta M} \cdot M_{\text{max}} = 5040 + 480 \cdot 9.1 = 9400 \text{ rpm} \]

The extreme working point should of course be used in the calculation (max. speed and max. torque), since the speed-torque line of the winding must run above all working points in the speed / torque diagram. This target no-load speed must be achieved with the maximum voltage (18 V supplied by the control (LSC), (voltage drop of the power amplifier of the LSC 6 V), which defines the minimum target speed constant \( k_{n, \text{th}} \) of the motor.

\[ k_{n, \text{th}} = \frac{n_{\text{th, max}}}{U} = \frac{9400}{18} = 522 \frac{\text{rpm}}{V} \]

Based on the calculation, motor 110162 is chosen which corresponds to the winding with the next highest speed constant (689 rpm / V) and has a second shaft end for mounting the encoder. The winding’s higher speed constant compared to the target value means that the motor runs faster than required at 18 V which, however, can be compensated for by the controller. This selection also ensures that there is a speed regulating reserve of more than 20 %. Thus, even unfavorable tolerances are not a problem.

The torque constant of this winding is 13.9 mNm / A. The maximum torque corresponds to a peak current of

\[ I_{\text{max}} = \frac{M_{\text{max}}}{k_M} = \frac{9.1}{13.9} < 0.7 \text{ A} \]

This current is lower than the maximum current (2 A) of the controller (LSC).

Therefore, a gear motor combination has been found that fulfills the requirements (torque and speed) and can be operated with the controller provided.

<table>
<thead>
<tr>
<th>Motor</th>
<th>( M_{\text{cent}} )</th>
<th>Suitability</th>
</tr>
</thead>
<tbody>
<tr>
<td>S2322, 6 W</td>
<td>13 mNm</td>
<td>Rather too strong, long</td>
</tr>
<tr>
<td>A-max 22, 6 W</td>
<td>7.5 mNm</td>
<td>Good</td>
</tr>
<tr>
<td>A-max 19, 2.5 W</td>
<td>4.4 mNm</td>
<td>Too weak</td>
</tr>
<tr>
<td>RE-max 21, 6 W</td>
<td>8 mNm</td>
<td>Good</td>
</tr>
</tbody>
</table>

![Graph of 6 Watt Motor](image)